Modelos de fuente sismica finita

Modelo de falla circular

Modele de Haskell

# Nacimiento de la dinamica de la fuente

# A principios de los años 1970 :

- Aki (1967) Scaling law of earthquake spectra
- Kostrov (1964, 1966) Circular crack, 2D crack, Energy
- Brune (1970) Circular crack body wave spectrum
- Madariaga (1976) put together all this.



2 Parametros: Mo R

No definen la velocidad de ruptura

# Ley de escalamiento de Aki



### Ley de escala de los terremotos

$$\log_{10} M_0(Nm) = 1.5M_w + 9.3$$

Magnitude (M <sub>w</sub> )	Moment (Nm)	Longueur (km)	Durée (s)	Glissement (m)
10	10 <sup>24</sup>	1000?	300?	100?
9	3.10 <sup>22</sup>	300	100	30
8	10 <sup>21</sup>	100	30	10
7	3.1019	30	10	3
6	10 <sup>18</sup>	10	3	1



Slip of a circular crack

$$D(r) = \frac{24}{7\pi} \frac{\Delta\sigma}{\mu} \sqrt{R^2 - r^2}$$

Average slip

$$\overline{D} = \frac{16}{7\pi} \frac{\Delta\sigma}{\mu} R$$



### Modelo de ruptura sismica circular (3D)





### Modelo de fisura circular estática

Deslizamiento 
$$D(r) = \frac{24}{7\pi} \frac{\Delta\sigma}{\mu} \sqrt{R^2 - r^2}$$

Deslizamiento medio

$$\overline{D} = \frac{16}{7\pi} \frac{\Delta \sigma}{\mu} R$$

Momento sísmico

$$M_0 = \frac{16}{7} \Delta \sigma R^3$$

Energia de deformacion

$$\Delta W = \frac{8}{7} \frac{\varDelta \sigma^2}{\mu} R^3$$

# Fundamentals of earthquake scaling Surface $M_0 = \Delta \sigma R^3$ R $R_0$ $\Delta\sigma R^2$ Signal $R_0^2$ Mo t R $\mathbb{R}^2$ Spectrum R<sup>3</sup> $R_{0}^{3}$ **R**<sup>-1</sup> $R_0^{-1}$

# Fundamentals of earthquake scaling Surface R $R^2$ R Velocity Displacement Signal Signal R Acceleration Signal $\mathbb{R}^2$ Spectrum R<sup>3</sup>

**R**<sup>-1</sup>

Modelo de escalamiento de la fuente

Deslizamiento medio  $\overline{D} = \frac{16}{7\pi} \frac{\Delta \sigma}{\mu} R$ 

Momento sísmico

$$M_0 = \frac{16}{7} \varDelta \sigma R^3$$

Frecuencia esquina

$$f_c = 0.37 \frac{\beta}{R}$$

Momento vs. frecuencia

$$M_0 \propto f_c^{-3}$$

# Escalamiento de momento y corner frequency





Frecuencia f

# Modern test of earthquake scaling law

Prieto, Shearer and Vernon, JGR, 2004



# Spectral analysis of California earthquakes



# Modern tests of earthquake scaling law



Test by Prieto et al JGR, 2004

$$f_p / f_s = 1.6$$

### Circular crack model

 $f_p / f_s = 1.7$ 

(Madariaga, 76)

# The Tocopilla Earthquake of 21 November 2007



In red PBO stations used for this study

#### The Tocopilla earthquake sequence in Northern Chile



### Spectral stack of a set Tocopilla aftershocks



From Lancieri et al (GJI 2012)

### Accelerograms of the main Tocopilla earthquake



Espectro de desplazamiento del Terremoto de Tocopilla de 2007 observado en 4 estaciones de la red PBO



From Lancieri et al (GJI 2012) and Peyrat et al (GJI 2010)

# How to model an earthquake: Maule 27 Febrero 2010





## **Central Chile Seismicity since 1906**



**Central Chile** 

### Mw>7.8

From Campos et al, 2002

# Preseismic deformation from GPS



 We would then conclude that the southern part of the Concepción– Constitución
gap has accumulated a slip deficit that is large enough to produce a very large earthquake of about Mw= 8.0– 8.5. »

This is of course a worst case scenario that needs to be refined by additional work.

(Campos, Ruegg, Vigny, R.M. et al, 2002, 2003, 2009)

### Ground displacement from GPS stations for the Maule earthquake of 2010



### Static GPS observation of the Maule 2010 earthquake



Rupture zone 400 km

Vigny et al, Science, 2011

Moreno et al, EPSL, 2012

# Vertical displacements measured by GPS



Hinge line

Color diamonds Vertical displacement of biological markers

(Farias et al, 2010)

From Vigny et al, 2011

# Inversion of Geodetic slip distribution



# Modelling the near field GPS data for the Mw 8.8 Maule 2010 earthquake



From Vigny et al Science (2011)

# Maule 2010: geodetic versus Far field BW inversion

Slip inverted from GPS

Slip Inverted from Far field body waves



Moreno et al (EPSL, 2012)

Pro, Buforn, Madariaga (EGU 2013)

# Maule 2010: Far field Body wave inversion

10





# Ground velocity inversion from cGPS Uses AXITRA for synthetics



#### Ruiz Mada Ragiz et alb Earthquake Spectra, 2012

# Postseismic deformation after Maule

Horizontal cumulated displacement (cm) over 4 years : between M 8.8 Maule Earthquake and 2014.



Use of stacking and backprojection for modelling High frequency features

# Low and High Frequency features of Maule 2010 Uses Backprojection



# Use of seismic antennaes for stacking



### Use of a seismic receiver antenna

Example of Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion



#### From SPUD in IRIS Data Center

http://ds.iris.edu/spudservice/data/1586357

Ruiz et al, EPSL 2013



# Example of Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion



### Example of Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion

Far field body wave modellig





SH

### Example of Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion

Observed and synthetic interferogram



### Available data from the IRIS data center Wilber III application



Red US array

25 Marzo 2012 Constitucion EQ



Displacement record « section »

Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion

Traces were aligned by Cross correlation

### Displacement record « section »



madariag /home/madariag/Chile/obspyDMT\_2016\_Cours/Data\_M001leg6/2012-03-25\_2012-03-26/20120325\_1/BH\_FMW//de55121:39:17 2016

### Displacement record « filter » AAM (Michigan)

Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion



#### madariag /home/madariag/Chile/obspyDMT\_2016\_Cours/Data\_Mauleg6/2012-03-25\_2012-03-26/20120325\_1/BH\_S04W//de50102:29:24 2016



# Velocity record « section »

Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion



### Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion

5 velocity seismograms of the US array

Ρ sP



Michigan

madariag /home/madariag/Chile/obspyDMT\_2016\_Cours/Data\_iddulice§\$/2012-03-25\_2012-03-26/20120325\_1/BH\_H7MU/de\$50121:58:09 2016

## Velocity record « filter » AAM (Michigan)

Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion





Maule aftershock Mw 7.1 of 25/3/2012 near Constitucion

Sum the stack at different points on the source area

This is a constant latitude (-35.1) section





### Use of a receiver antenna

Example of Maule aftershock Mw 6.7 of 14/2/2011 near Constitucion

z 2011/02/14 03:40 M6.7 Z=17km



Example of stack at different frequencies



Time relative to origin (sec)



### Example of Maule aftershock Mw 6.7 of 14/2/2011 near Constitucion

#### Example of Maule aftershock Mw 6.7 of 14/2/2011 near Constitucion





ongitude [degrees]



#### 2nd order (energy) stack



# Back Projection: results

### US Array 0.3-1 Hz

### POLENET Array 0.3-1 Hz



# Teleseismic Kinematic Inversion and Back Projection



