

## GPS : HOW AND WHAT FOR ?

### What is GPS ?

Since the end of the 70's, one of the main concerns of the american "Department of Defense" (DoD), has been to conceive a system which will allow any element of the american army (planes, ships, submarines, tanks, ground troupes) to know their position precisely and instantaneously, anytime and anywhere on the earth surface. The Global Positioning System (GPS) was built to fulfill this task.

### Commercial applications

In essence, the GPS system is made of a constellation of 24 satellites orbiting at an average altitude of 20,000 kms, scattered on 6 orbital planes equally spaced. As a result, at least three satellites are always visible at anytime and from anyplace on earth. Each satellite emits a coded signal which contains essential informations like its position and the exact timing of the signal emission to earth. Therefore, nothing but a simple receiver is needed to measure the elapsed time between emission and reception of the signal. The satellite to station distance is simply deduced from this travel time. Three different measurements made on three different satellites give the three distances needed to determine the three coordinates of the station position : latitude, longitude, and altitude. This type of measurements is known as "pseudo-range" measurements in GPS jargon. Every satellite emits two types of pseudo-ranges : A precise code (P code) which enables a position precision of around 10 meters and a coarse code (C/A code) which allows a precision of around 100 meters. The precise code is encrypted to deny the precise positioning to anyone else than the american military. Therefore, the only precision available to civilian applications based on the pseudo-ranges measurements is this of the C/A code.

### Scientific applications

The precision achieved by pseudo-range measurements is not good enough for most of the GPS applications in geophysics. For plate tectonic for exemple, it is required that measurements be precise at the centimeter level (even millimeter), if one is to be able to detect motions of a few centimeters per year (or less) without having to wait

### *1-Pseudo-range codes and access policy of the DoD*

*Hence, there are two types of pseudo-distance which allow different precisions :*

- The C/A (Coarse Acquisition) code, available to all potential users, which allows a precision of around 100 m. It is this signal which is recorded in most commercial GPS receivers used for navigation purposes (ships, airplanes, and parisien taxis)*
- The P (Precise) code, encrypted to deny access to anyone else but the american army, which allows a precision of around 10 m. This P-code encryption scheme, known as "Anti Spoofing", was designed to deny access to potential ennemy at wartime but has been in fact activated permanently since the beginning of 1994.*

*Again, to prevent potential "hostiles" to be able to get precise positions from GPS, the system was built with the capacity to degrade its precision. This is achieved by artificial degradation of the precision with which a certain number of parameters are broadcasted by the satellites. For any of those numbers, the last "byte" which contains the final digits (and therefore the full precision) is deliberately jammed, that is single bit positions are exchanged using an unknown algorithm. This dithering, known as Selective Availability, affects first the clock of the satellites which gives the time tag for signal emission, and second the satellite orbits which give the position of the emission point. In practical, it is possible to go around this problem by using differential GPS. This technique consists in using a reference station which position is known with accurate precision. At every momment, the difference between the wrong measured position and the true known position is radio broadcasted as a correction valid in the whole area of the reference station.*

for hundred of years to generate sizeable displacements. Then, a different technique is applied. It consists in acquiring measurements of the satellite-station distance directly on the carrier wave of the GPS signal (phase measurements). In principal it is similar to pseudo-range measurements, except that the wavelength (or characteristic size) of the signal is considerably reduced, which allows a far better precision.

## Phenomenon affecting phase measurements precision

In addition to volunteer degradation of the signal quality by the American military, there are a number of natural causes which limit the precision of the GPS positioning. Among them and by order of importance : Ionospheric and Tropospheric refraction, GPS satellite orbits precision, multipath effects, and position of the phase center of the GPS antennas. Some of these effects can be accounted for in a more or less satisfying way, others are almost out of control.

### Ionospheric refraction

The Ionosphere, as stated by its name, is an envelope around the Earth made of electrical particles (ions) which orbit at an altitude higher than 20 km. The carrier wave of the GPS signal has to travel through this layer on its way from the satellite to the station. The simple fact that this layer is non neutral implies a perturbation of the velocity of any electromagnetic wave going through it. The amplitude of this perturbation is related to the wavelength and to the density of electric particles in the medium, which density is unknown and changes in space and with time. Therefore, the travel time of the GPS wave will be affected by an unknown quantity, named ionospheric delay, and finally the inferred distance between the satellite and the station will be wrong.

The solution consists in emitting two different waves on two different frequencies. Each of them will be affected by a different amount, and the comparison will give an evaluation of the ionospheric delay for all wavelengths. It is for this very reason that the GPS system is "dual-frequency", which means that two slightly different waves are emitted (1.575 GHz and 1.228 GHz). Nevertheless, whenever the Ionosphere is not in a steady state, in case of a solar storm for example, the evaluation of the ionospheric delay remains approximative and the precision of the measurement questionable.

### Tropospheric refraction

In the same way, the travel time of the GPS wave is affected by the water vapor contained in the lower atmospheric layer (from 0 to 10 km altitude) : the Troposphere. Therefore, it would be necessary to

### 2-Carrier beat phase measurements

*The wavelength, or characteristic size of the signal, is reduced from 30 m for C/A-code and 3 m for P-code to 19 cm for the carrier wave of the first one and 24 cm for the carrier of the second one. It is possible to measure a time shift between two waves with an accuracy up to a fraction of one wavelength. Therefore, measurements based on the carrier wave phase can achieve a sub centimetric precision. Nevertheless, this technique has a major drawback : phase measurements are fundamentally ambiguous. When different (therefore identifiable) crests follow each other in the pseudo-range signal, nothing allows the identification of one wavelength from the previous or the following one : they are all strictly identical. In other words, the actual number of oscillations from the satellite to the station remains unknown. What is known is the number of oscillations which separate two measurements made on the same satellite at two different times. Therefore, there is no direct access to the distance satellite-station and then no real time direct measure of the station position. On the other hand, after continuous measurements have been recorded on all available satellites for a given time, one disposes of a large number of equations (as many as recorded measurements) for a small number of unknowns (3 for station position and 1 for each satellite-station distance at the first measurement). The technique consists then in acquiring as many measurements as possible, recording them, and processing the equations system with a computer while back in the laboratory. Also, to eliminate the inauspicious effects of the Selective Availability, it is necessary to combine data from different stations (again differential GPS). This allows to cancel the errors from the satellite clocks by paying the cost of losing absolute positioning. Therefore, only distances between stations are known and not station positions. In geodesy, those distances are called baselines and have three components : one vertical component which corresponds to the altitude difference between the stations, and two horizontal components which are the distances between the stations along the North-South and East-West directions.*

know this quantity with precision along all the travel path followed by the wave. This turns out to be an impossible task, even with the dual frequency system. Since the perturbation introduced is more complicated than a simple time ratio related to water

vapor percentage, the differentiation between the two waves does not produce the requested information : the tropospheric delay. There are different techniques to adress this problem, neither of which being fully satisfactory. The simplest one consists in simply putting an additional unknown in the computations : the tropospheric delay itself. Nevertheless, since this parameter changes along with meteorological conditions, it is necessary to modify its value as time passes (every two hours for exemple). Eventually, this leads to the introduction of many unknowns, which makes the computations less stable and the results more questionnable.

In practical this problem is important when meteorological conditions and tropospheric layer thickness are different from one location to another. The baseline between two stations, one being located near the sea (at zero altitude) with a high hygrometric level and the other one in high mountain ranges with dry air, will be mostly affected. Finally, this error will show up mostly on the vertical component of the baseline (the stations altitude difference). The horizontal components will be less affected because the errors will more or less average out since the satellites cover all azimuthal directions (when the elevation coverage is restricted to the above horizon satellites). From the theoretical point of view, instruments which allow to directly measure the water vapor contains along the GPS wave path are currently under experimentation. Yet, it is to soon to tell if such measurements, based on sky brilliance temperature, can be made accurate enough for precise GPS applications.

### GPS satellite orbits precision

Clearly, if an error is made on the satellite position, this error will directly map into the station position since it is inferred from the satellite to station distance. Again, the baseline between two stations will be less affected than the station positions. If the two stations are not too far away, the satellite position error (identical for the two stations) will cancel out when differenciating. Nevertheless, the rule of thumb is that the relative error on the orbit equals the relative error on the baseline. GPS satellite orbits can be computed very accurately but they are broadcasted by the american military with a lousy precision of only 200 m. Over an average altitude of around 20,000 km, this leads to a proportional error of  $10^{-5}$  (10 ppm), which is an error of 10 cm on a 10 km baseline ! Such a large error is totally unacceptable for precise GPS positioning. Therefore, it absolutely necessary to recompute GPS satellite orbits with precise

orbitographic softwares. This is done by using GPS data acquired at fiducial stations scatered on the earth surface and maintained for this purpose by the International GPS Service (IGS), on behalf of the international scientific comunity. Those recomputed orbits are precise at 20 cm, or  $10^{-9}$  (1 ppb), which leads to an error reduced to 1 mm on a 1000 km long baseline.

### Multipaths

Those phenomenoms are among the most difficult to seize. It is very easy to see that any reflecting object disposed close to the GPS antenna may reflect part of the signal coming from the satellite towards this antenna. Acting exactly as a mirror creating one's image when one looks at it, the reflecting object will create an image of the GPS antenna. It is then the position of this fake antenna which is measured instead of the one of the true antenna. Moreover, as the satellite is moving on its orbit, the reflection angle on the "mirror" changes, and the antenna image moves. Then, it is the positon of a moving fake antenna which is being measured ! It is extremely difficult to analyse theoretically the impact of such and such potentially reflecting object. It is possible to shield the antenna against such parasite reflections, but the shield has to be uncomplete since the direct signal has to reach the antenna. The only solution is to avoid as much as possible multipath effects by eliminating all potentially reflecting objects from the neighbourhood of the antenna, which is not so easy when one realizes that the ground itself is such a reflector !

### The position of the GPS antenna phase centers

When measuring the position of a GPS antenna, what is it that we actually measure ? Actually, the hart of a GPS antenna is basically made of an electric wires coal inside which the electromagnetic wave signal is converted into an electric current. It is the position of the very point where the conversion occurs (named antenna phase center) which is measured. But such a point is not materially defined. It is a virtual point which position depends on the angle of incidence of the wave with respect to the wire coal, that is with the antenna itself. The phase center, and therefore the antenna measured position can move several centimeters apart, depending on where the signal comes from, that is where the satellites are ! Here again, the error will be moreorless averaged out

since GPS signals come from almost everywhere, thanks to the good spatial coverage of the satellites. Nevertheless, and because satellites cannot be recorded below our feet across the Earth, a systematic shift in the altitude is inevitable. It is possible to map the displacements of an antenna phase center in the laboratory. Nevertheless, such measurements are very difficult to make and corrections from them are to be used with caution. On a practical point of view, the problem is solved by using only identical antennas for a given survey and by orientating all of them towards the same direction. This will make all antenna phase centers move in the same direction at the same time, and then baselines will remain constant although the points at their ends will change position. Here again were are conducted to doing relative positioning instead of absolute positioning.

### **Plate tectonics measured by GPS**

The Wegener hypothesis of continental drift was confirmed twenty years ago and since then by numbers of geophysical observations. Among those, the most striking is the discovery of magnetic strips, parallel to the ridge and successively positive and negative, "printed" in the ocean floors. Ocean floors are made of the lava flowing out of the ridge. As they cool down, the rocks trap the current Earth magnetic field. Because inversions of the magnetic field polarity occurred many times in the past, successive negative and positive values of the field are captured. Therefore, the "zebra skin" of the ocean floors gives a strong evidence for oceanic expansion and for plate tectonics. Velocity of this continental drift were estimated from the age of these strips and their size. Similarly, it is possible to estimate the shift in between two sides of a given structure separated by a fault (an old volcano or a fossile river bed for example). Again, the evaluation of the age of the event will give an estimation of the speed along the fault.

The major drawback of these methods lies in the fact that they give an estimation of the velocity averaged on the geological time scale. Instantaneous velocities can be very different from their average on long time scales. Therefore, it is essential that present day velocities can be measured directly. Among all the existing tools of geodesy (ground theodolites and distance meters, space devices like VLBI, SLR, LLR, DORIS), GPS is very well suited to the measurement of the deformation in a given area. Thanks to its good precision, to its relatively low cost, to its operating facility, and to the fact that

it does not require site inter-visibility, it is possible to make a large number of measurements quickly and cheaply on the studied area.

The principle is quite simple. A geodetic point is materialized by a reference mark, typically a metal pin dug in an outcrop solidely tied to the bedrock. Using a tripod and an optical device it is possible to center the GPS antenna exactly on top of the bench mark, at a determined height. Therefore, the position of the reference mark can be easily deduced from the measured position of the GPS antenna. By remeasuring the position of the benchmark after a given time span it is possible to detect a displacement and deduce a velocity. The deformation in a given area will be deduced from the displacements of many points measured in the area. These many points just make a geodetic network. Practically, since we must do a large number of differential measurements to achieve a good precision, it is necessary to measure all points simultaneously during many hours and even several days. Typically, at all stations, one measure will be recorded every 30 seconds on all available satellites at every moment during 3 full days. This represents an average of 30,000 to 40,000 measures by point. Of course, the total measurement time span is given by the required precision of the survey : 3 days for sub-centimetric precision over large scale networks, but only one hour for very short baselines (less than 1 km) or if sub-decimetric precision is enough.

### **Other applications**

GPS is a formidable tool for positioning, and the simple fact of being able to measure the position of a given point with a very good accuracy opens the way to a great number of scientific applications.

Surveying an active fault

Naturally, the american scientists were the first to envision the application of GPS abilities to geophysical applications. On the other hand, one of the major concerns of the authorities in this field is to study the seismic hazards in California. In this area of the world, the sliding of two tectonic plates along the San Andreas fault induces many devastating earthquakes like those of San Francisco and Los Angeles lately. By measuring the positions of points regularly scattered on both sides of the fault, and by looking at the motions of those points, it is possible to map the fault very accurately. The analysis of ground deformation in the vicinity of the fault gives basic informations on the fracture depth,

the length of the active segments, and allows to define areas where the seismic risk is the more important.

Moreover, immediately after an earthquake, the GPS measure gives access to the total displacement of the ground generated by the quake. This information is decisive for the study of the fundamental mechanisms which govern seismic rupture. Lastly, it is even possible to measure the positions of GPS points during an earthquake. By computing the point positions at every measurement, one can literally see the points moving during the couple of minutes the quake lasts. If those points are well placed, one can see the propagation of the rupture along the fault. Here again those informations allow to analyse the seismic waves propagation and the induced ground motions. This type of network, dedicated to monitoring an active fault, are now being developed in different areas around the world : Japan, Indonesia, and Turkey for exemple.

#### Monitoring volcanos

In the same way, it is possible to observe the deformations of the cone of an active volcano. With just a few GPS points adequately placed and measured continuously, it is possible to follow day after day the deformations due to the rise of the lava flow. These measurements are usefull to volcanologist to quantify the phenomenons associated with an eruption. One can also envision to acquire some predictive capabilities, once these phenomenons are well understood. Presently, such GPS measurements are conducted on different volcanos like "le Piton de la fournaise" and "la Souffrière" in the french Antilles, and the Merapi in Java, Indonesia.

#### "Post glacial rebound" and its implications on global change

Since a couple of years, it has been suspected that the sea level is constantly rising. Although the numbers may be very small, a couple of millimeters per year at most, this is a major concern for the whole planet. It is very difficult to confirm this hypothesis and to find the precise numbers because sea level variations are mixed with continents uplift or subsidence. Locally, those tectonic motions can very well induce a sea level decrease, even though the ocean surface is globally rising (if the shore is rising faster for example). On

the other hand, if the sea level is rising, the water must come from somewhere. It was suggested that global warming of the planet would "melt" the polar ice sheets, and therefore free an important amount of liquid water in the oceans. Although it would take thousands of years of warming to start to really melt the Antarctic ice sheet, a small change of the thermal conditions can generate large variations in the speed of the glaciers. This could easly affect the total amount of water released in the ocean. By liberating water, such a phenomenon would generate a decrease of the mass of the ice sheet. An uplift of the continent underneath would therefore take place as its load decreases. Such an effect took place in the past in the Canadian Laurentides and in northern Europe during and after the deglaciation periods. Using GPS, it is possible to measure the possible uplift of the Antarctic continent induced by the ice sheet mass decrease. A quantification of the uplift would allow a quantification of the amount of water send in the oceans, and therefore assess the risk of sea level rise. Such measurements started a couple of years ago and results are expected to come out in the near future.

#### Measuring of the geoid

Because of density anomalies inside the planet, the Earth gravity field is not the one of an homogenous sphere flattened at the poles. On the opposite, it shows swells and holes in accordance with the density of the rocks in the crust and below, and the elevation of the topography. Where the Earth surface is covered by oceans, the liquid water goes freely where the gravity is stronger, to reach an equilibrium at an higher altitude until the gravity is equal along the water surface. The ondulated surface thus generated is called the Geoid. Of course the geoid exists also over the continents, although it is not materialized by the presence of water.

The knowledge of the Geoid is of first importance to geophysicist. Because it is affected by masses deep in the Earth mantle, the Geoid gives precise indications on the density and composition of the deep interior of the planet. Over the oceans, the Geoid is known from altimetric satellites which simply measure the altitude of the sea level. Nevertheless, and because it is not materialized over solid surfaces, the continental Geoid is difficult to measure and remains not very well known. Now, the GPS system, because it uses satellites which orbit around the Earth center of mass, gives the position with respect to this reference system. That is to say that one knows the

distance between a GPS point and the Earth center. Then, it is enough to know the altitude of this point (ie. its relative height to the ocean level) and the difference between the two is simply the Geoid !

### Measuring of erosion

Last, it is possible to use the GPS system in a slightly different manner. This application uses the navigation reasoning, but keeps the principle of the phase measurements which allow accurate enough positioning. By making measurements very frequently, it is possible to follow the trajectory of a mobile receiver. Each measure gives the position (latitude, longitude, and altitude) of the receiver as a function of time. Because there is only one measure for each position, the latter is known with a degraded precision. Nevertheless, the receiver position at a given time is related by its velocity to its positions just before and immediately after. Finally, it is possible to reconstruct the trajectory of the receiver with a sub decimetric precision. Doing this, it is possible to make a precise topographic map (altitude versus latitude and longitude) of a given area covered by a GPS receiver placed on a car or on human back. This is very easy to do on the sea shore, where it is possible to map the sand dunes and the inter tidal area uncovered by the sea at low tide. It is even possible to map the topography of the sand banks below the water level by coupling the GPS receiver to a depthmeter (SONAR). By measuring

### *3-Cost of GPS receivers*

*A commercial receiver used for navigation purposes will be able to measure only the coarse pseudo range distances coded on one of the two frequencies. Such receivers are available from 1500 FF or 300 USD. On the opposite, dual frequency receivers able to measure both pseudo-range and phase data on both carrier waves cost up to 150,000 FF or 30,000 USD. There is an intermediate category of receivers which allow relatively precise positioning without being excessively costly. Those are the single frequency receivers, which measure pseudo-range and phase data on only one of the two wavelength. Acquiring data only on the frequency with the higher signal/noise ratio, those receivers are built with relatively cheap electronic.*

these topographies at regular interval, or immediately after a storm, it is possible to directly monitor the effects of slow and continuous erosion or catastrophic events, as well as quantify the amount of material (sand) involved and the paths it followed. These techniques are presently being tested on the french northern sea shore.

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