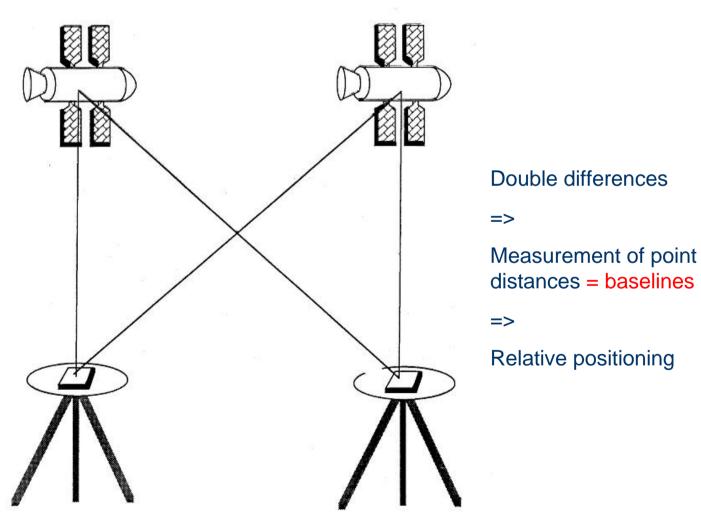
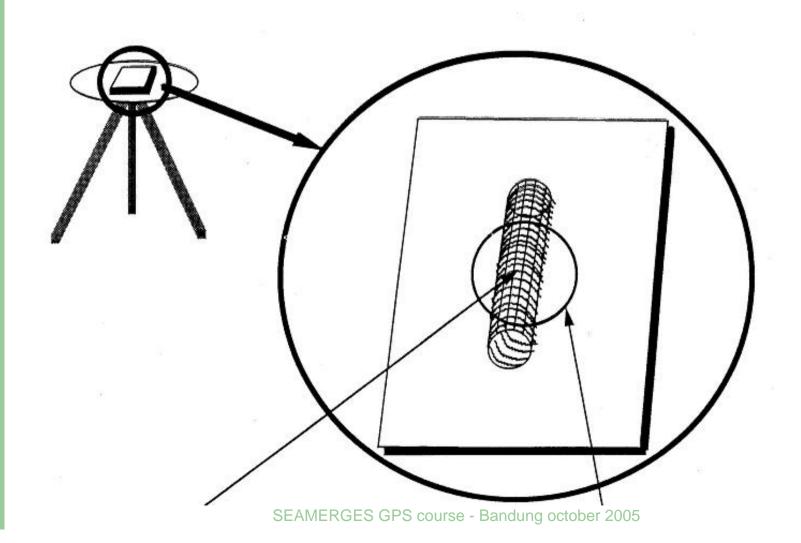
#### **GPS** uncertainties

- Relative/ vs. absolute positioning
- Position precision limitations
- Velocity uncertainties
- Accuracy vs. Precision
- Mapping in a reference frame

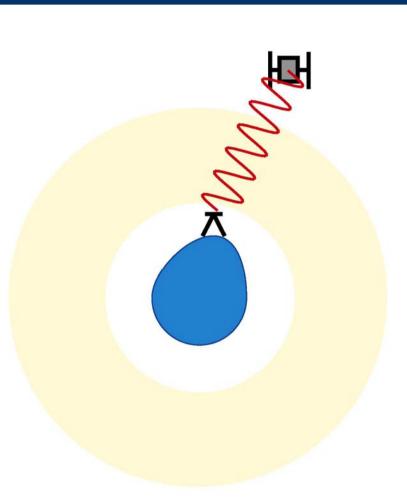
### **Double differences**



### Phase center offset and variations



# **lonosphere sketch**



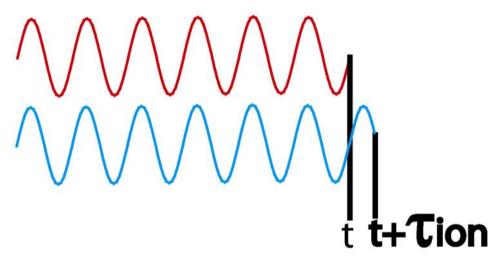
Correct measurement in an empty space

But the ionosphere perturbates propagation of electric wavelength .....

... and corrupts the measured distance

... and the inferred station position

### **lonosphere theory**



Ionospheric delay  $\tau$ ion depends on :

- ionosphere contains in charged particules (ions and electrons) : Ne
- Frequency of the wave going through the ionosphere : f

 $\tau_{\text{ion}} = 1.35 \ 10^{-7} \ \text{Ne} \ / \ \text{f}^2$ 

#### **lonosphere**: solution = dual frequency

Problem: Ne changes with time and is never known

solution: sample the ionosphere with 2 frequencies

$$T_{ion_1} = 1.35 \ 10^{-7} \ Ne \ / \ f_1^2$$
  $T_{ion_2} = 1.35 \ 10^{-7} \ Ne \ / \ f_2^2$ 

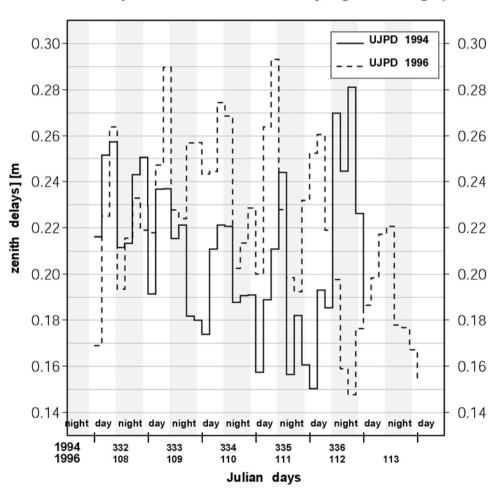
$$T_{ion_2}$$
 -  $T_{ion_1}$  = 1.35 10<sup>-7</sup> Ne (1/ $f_2^2$  - 1/ $f_1^2$ )

Ne = 
$$\left[ \tau_{\text{ion}_2} - \tau_{\text{ion}_1} \right] / 1.35 \cdot 10^{-7} \left( 1/f_2^2 - 1/f_1^2 \right)$$

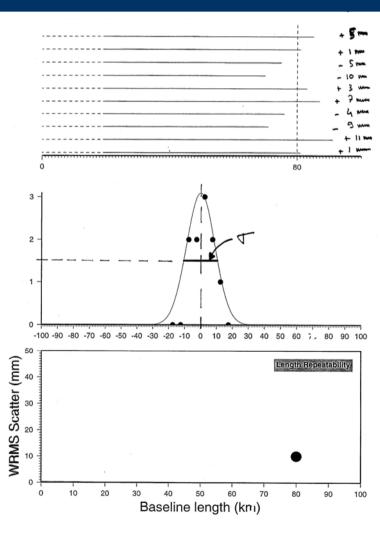
Dual frequency GPS to quantify ionospheric delay Make ionoosphere TEC maps with GPS

# **Troposphere**

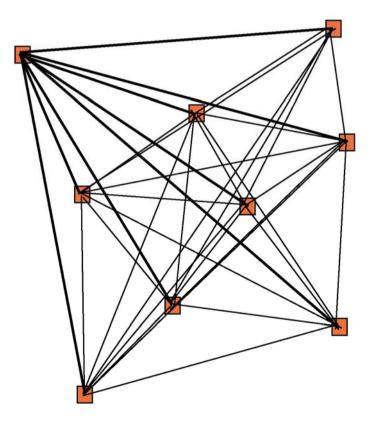
#### Atmospheric Parameters at Ujung Pendang (Indonesia)



# **Precision and repeatability**



#### **Network repeatabilities**



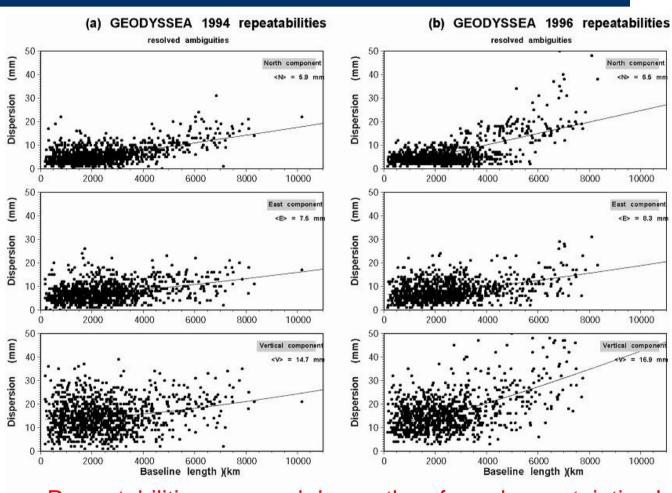
Network of N points (N=9)

(N-1) (=8) baselines from 1st station to all others

(N-2) (=7) baselines from 2nd station to all others => subtotal = (N-1)+(N-2)

total number of baselines = (N-1)+(N-2)+...+1= N(N-1)/2 (36 in that case)

### Typical repeatabilities (60 points => ~1800 bsl)



Repeatabilities are much larger than formal uncertainties!

#### From position to velocity uncertainty

If one measures position  $P_1$  at time  $t_1$  and  $P_2$  at time  $t_2$  with precision  $\Delta P_1$  and  $\Delta P_2$ , what is the velocity V and its precision  $\Delta V$ ?

$$V = (P_2 - P_1) / (t_2 - t_1)$$

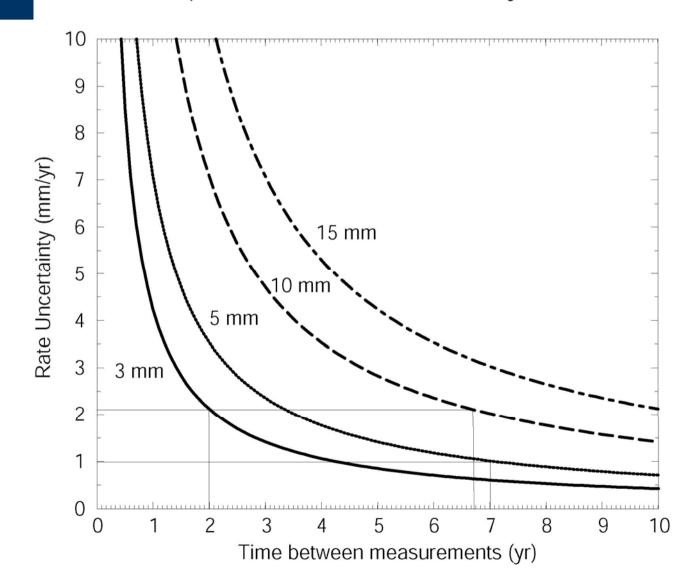
$$\Delta V = (\Delta P_2 + \Delta P_1) / (t_2 - t_1)$$

Uncertainties don't add up simply, because sigmas involve probability.

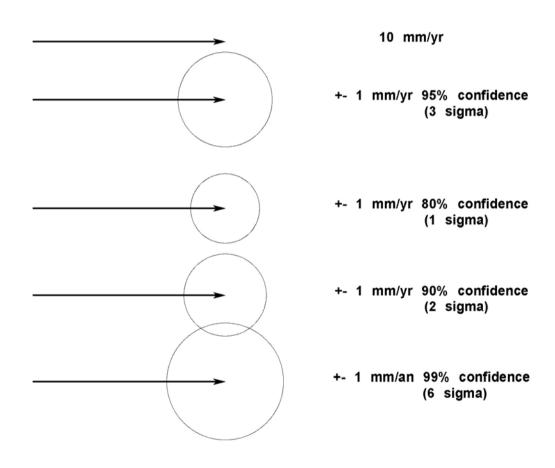
$$\Delta V = \left[ (\Delta P_2)^2 + (\Delta P_1)^2 \right]^{1/2} / (t_2 - t_1)$$

### **Velocities uncertainties**

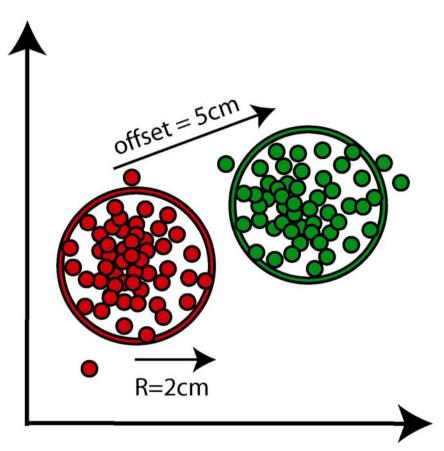
Expected Precision of the Velocity Estimates



# **Velocities ellipses**



## **Accuracy vs. precision (1)**



Fix point : measure 1 hour every 30 s

=> 120 positions

with dispersion ~+/- 2 cm

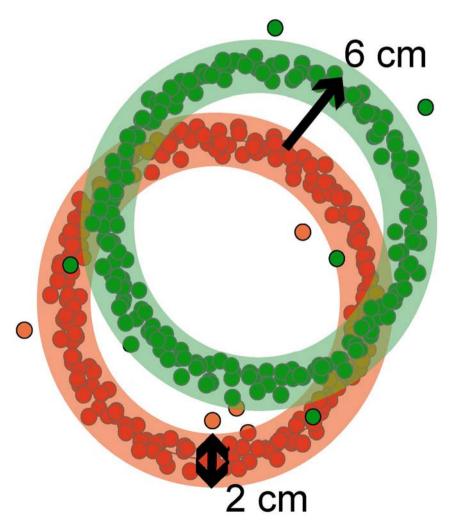
5 hours later, measure again 1 hour at the same location

=> Same dispersion but constant offset of 5 cm

Precision = 2 cm

Accuracy = 5 cm

# **Accuracy vs. precision (2)**



Measure path, 1 point every 10s

=> 1 circle with 50 points
10 circles describe runabout
with dispersion ~ 2 cm

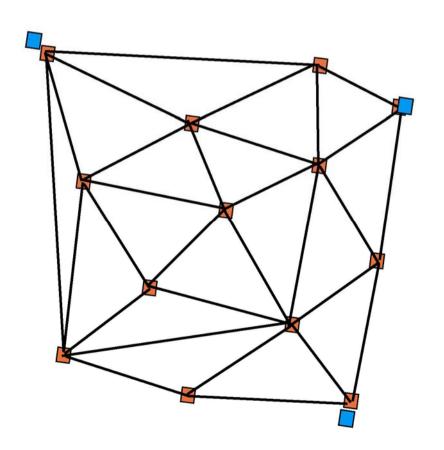
Next day, measure again

=> Same figure but constant offset of 6 cm

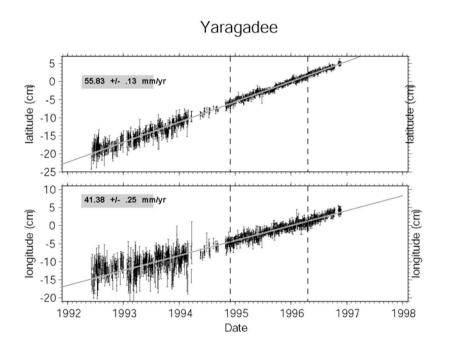
Precision = 2 cm

Accuracy = 6 cm

# Mapping in a reference frame (sketch)



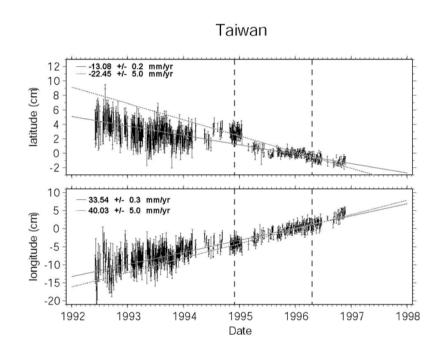
# Mapping in a reference frame (1)



Constraining campaign positions (and or velocities) to long term positions (and or velocities) works fine ...

... when station displacement is constant with time

## Mapping in a reference frame (2)

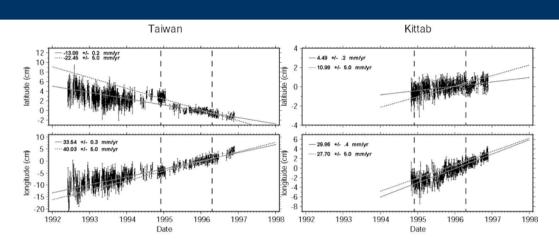


Constraining campaign positions (and or velocities) to long term positions (and or velocities) does not work

. . .

... when station displacement is not constant with time

# Mapping in a reference frame (3)



#### some stations are better than others ...

